

5675154

B.Tech. DEGREE EXAMINATION JANUARY 2023

Fifth Semester

Information Technology

THEORY OF COMPUTATION

(2013 – 14 Regulations)

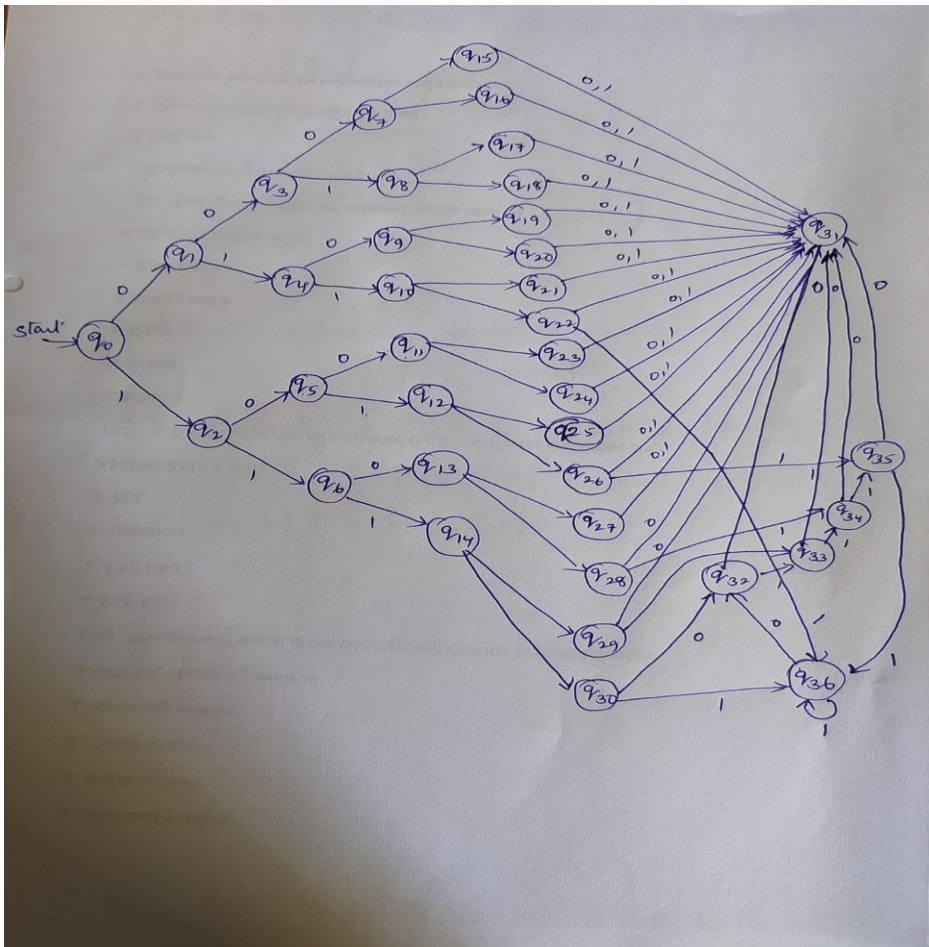
Time: Three hours

Maximum: 75 marks

SECTION A – (10 * 2 = 20 marks)

Answer ALL the questions.

1. Give the DFA accepting the language over the alphabet 0, 1 that has the set of all strings such that each block of 5 consecutive symbol contains at least two 0's.



2. Compare the functionalities of Mealy and Moore machines.

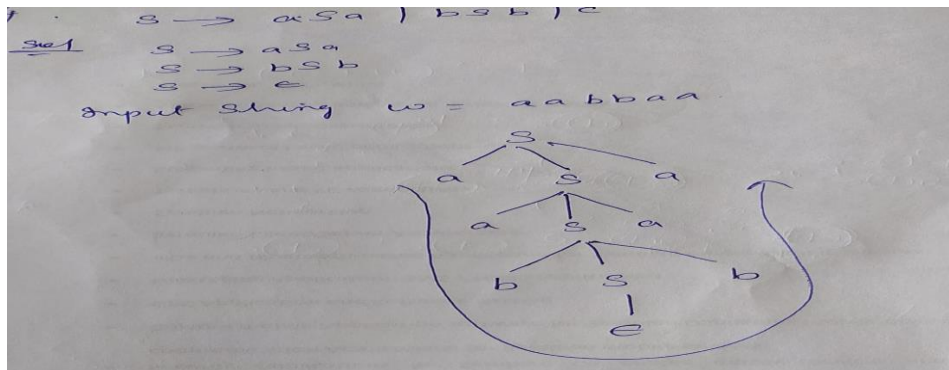
| Mealy machine | Moore machine | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--|---------------|-------------|-------------|-------------|--|-------|--|-------|--|--|-------|--------|-------|--------|-------------------|-------|---|-------|---|-------|-------|---|-------|---|-------|-------------|-------------|-------------|-------------|--|---------------|------------|--|--------|-------|-------|-------|-------|-------|---|-------|-------|-------|---|-------|-------|-------|---|-------|-------|-------|---|
| <p>1. Each and every transition contains the output.</p> <p>2. It consists of 6-tuples $M = (Q, \Sigma, \Delta, \delta, \lambda, q_0)$ where: Q - finite set of states Σ - finite set of input symbols. Δ - finite set of output alphabets δ - set of input transitions λ - finite set of output transitions q_0 - starting state</p> <p>3. Transition diagram:</p> <p>4. Transition Table</p> <table border="1"> <thead> <tr> <th rowspan="2">Present state</th> <th colspan="4">Next state</th> </tr> <tr> <th colspan="2">$a=0$</th> <th colspan="2">$a=1$</th> </tr> <tr> <th></th> <th>state</th> <th>output</th> <th>state</th> <th>output</th> </tr> </thead> <tbody> <tr> <td>$\rightarrow q_0$</td> <td>q_0</td> <td>0</td> <td>q_1</td> <td>1</td> </tr> <tr> <td>q_1</td> <td>q_1</td> <td>0</td> <td>q_2</td> <td>1</td> </tr> <tr> <td>q_2</td> <td>\emptyset</td> <td>\emptyset</td> <td>\emptyset</td> <td>\emptyset</td> </tr> </tbody> </table> | Present state | Next state | | | | $a=0$ | | $a=1$ | | | state | output | state | output | $\rightarrow q_0$ | q_0 | 0 | q_1 | 1 | q_1 | q_1 | 0 | q_2 | 1 | q_2 | \emptyset | \emptyset | \emptyset | \emptyset | <p>Each and every states contains the output.</p> <p>- It consists of 6-tuples. $M = (Q, \Sigma, \Delta, \delta, \lambda, q_0)$.</p> <p>- Transition diagram:</p> <p>- Transition Table</p> <table border="1"> <thead> <tr> <th rowspan="2">Present state</th> <th colspan="2">Next state</th> <th rowspan="2">output</th> </tr> <tr> <th>$a=0$</th> <th>$a=1$</th> </tr> </thead> <tbody> <tr> <td>q_0</td> <td>q_3</td> <td>q_1</td> <td>0</td> </tr> <tr> <td>q_1</td> <td>q_1</td> <td>q_2</td> <td>1</td> </tr> <tr> <td>q_2</td> <td>q_2</td> <td>q_3</td> <td>0</td> </tr> <tr> <td>q_3</td> <td>q_3</td> <td>q_0</td> <td>0</td> </tr> </tbody> </table> | Present state | Next state | | output | $a=0$ | $a=1$ | q_0 | q_3 | q_1 | 0 | q_1 | q_1 | q_2 | 1 | q_2 | q_2 | q_3 | 0 | q_3 | q_3 | q_0 | 0 |
| Present state | | Next state | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | $a=0$ | | $a=1$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | state | output | state | output | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\rightarrow q_0$ | q_0 | 0 | q_1 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| q_1 | q_1 | 0 | q_2 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| q_2 | \emptyset | \emptyset | \emptyset | \emptyset | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Present state | Next state | | output | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | $a=0$ | $a=1$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| q_0 | q_3 | q_1 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| q_1 | q_1 | q_2 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| q_2 | q_2 | q_3 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| q_3 | q_3 | q_0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

3. Give English description of the following language $(0+10)^*1^*$.

This is the language of strings in which there are no two consecutive 1's except for possibly a string of 1's at the end.

4. Let G be the grammar with $S \rightarrow aSa / bSb / \epsilon$

Construct Parse tree for the input string $w = 'aabbaa'$



5. List the primary objectives of Turing machine.

The main advantages of the Turing machine is we have a tape head which can be moved forward or Backward and the input tape can be scanned. The simple logic which we will apply is read out each '0' Mark it by A and then move ahead along with the input tape and find out 1 convert it to B.

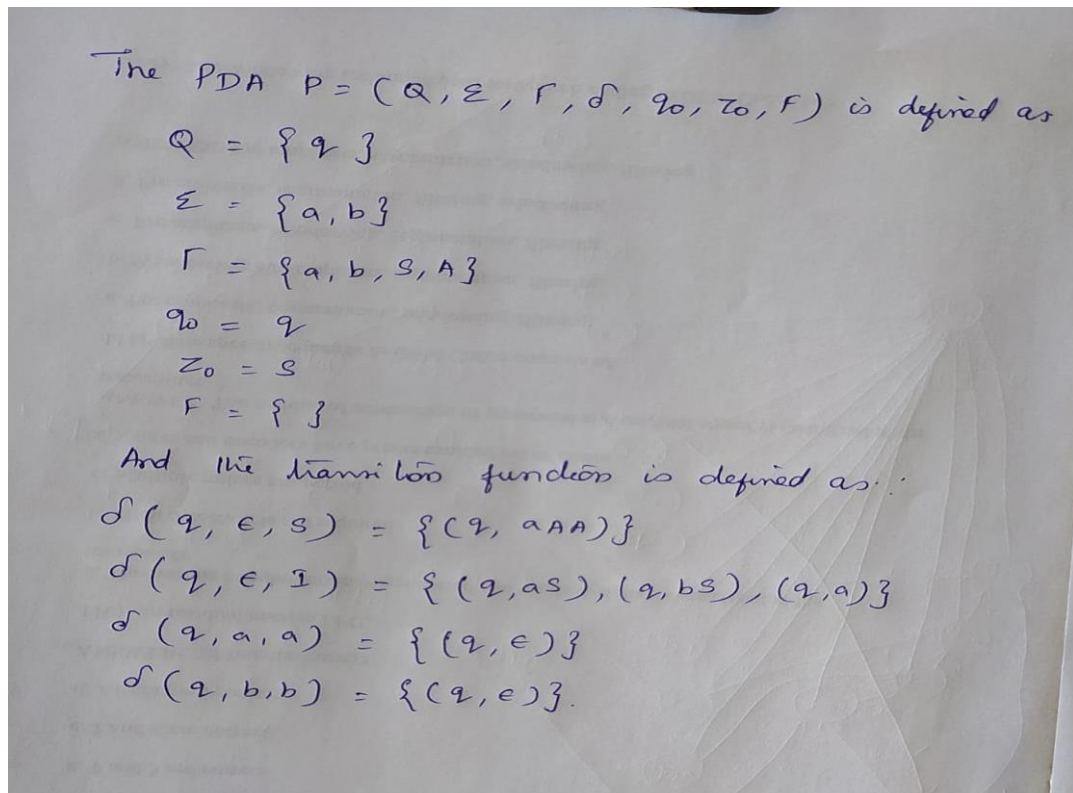
6. State when a problem is said to be undecidable and give an example of an undecidable problem.

A problem whose language is recursive is said to be decidable. Otherwise the problem is said to be undecidable. Decidable problem have an algorithm that takes as input an instance of the problem and determine whether the answer to that instance is "yes" or "no".

Eg. Of undecidable problems are (1) Halting problem of the TM.

7. Convert the following CFG to PDA.

$S \rightarrow aAA, A \rightarrow aS / bS / a.$



8. Does a Pushdown Automata have memory? Justify.

Yes. Finite automata can be used to accept only regular languages. Pushdown automata is a finite Automata with extra memory called stack which helps pushdown automata to recognize Context Free Languages.

9. Differentiate Top down and bottom up parsing approaches.

| TOP - DOWN PARSER | BOTTOM - UP PARSER |
|--|--|
| 1. This is top-down (LL) parser. | This is bottom-up (LR) parser. |
| 2. It attempts to find left most derivations for an input string. | It can be defined as an attempt to reduce the input string to the start symbol of a grammar. |
| 3. In this parsing technique we start parsing from the top to down (start symbol of parse tree to the leaf node of parse tree) in a top-down manner. | In this parsing technique we start parsing from the bottom to top (leaf node of parse tree to start symbol of parse tree) in a bottom-up manner. |
| 4. This parsing technique uses Left Most Derivation. | This parsing technique uses Right Most Derivation. |
| 5. The main leftmost decision is to select what production rule to use in order to construct the string. | The main decision is to select when to use a production rule to reduce the string to get the starting symbol. |
| 6. Eg. Recursive Descent parser or Predictive Descent parser. | Eg. Shift Reduce parser. |

10. Consider the following grammar

$$S \rightarrow Aa / b$$

$$A \rightarrow Ac / Sd / \epsilon$$

Eliminate the left recursion.

$$S \rightarrow Aa | b$$

$$A \rightarrow Ac | Sd | e$$

There is no immediate left recursion.

* To obtain the immediate left recursive substitute the S-productions in $A \rightarrow Sd$.

$$A \rightarrow Ac | Aad | bd | e$$

* Replaced as

$$A \rightarrow bd A' | A'$$

$$A' \rightarrow cA' | adA' | e$$

* Finally, we obtain

$$S \rightarrow Aa | b$$

$$A \rightarrow bd A' | A'$$

$$A' \rightarrow cA' | adA' | e$$

SECTION B – (5 * 11 = 55 marks)

Answer ALL questions.

UNIT – I

11. Design a NFA accepts the following strings over the alphabet {0, 1}. The set of all string that begins with 01 and ends with 00. Check for the validity of 011100 and 01100 strings and find its equivalent DFA.

Sol

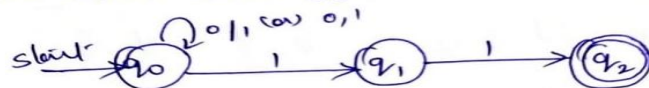
NFA: Non-Deterministic Finite Automata

- It is transition from more than one input symbols.
It is called as NFA.
- 5-tuple:
 $M = (Q, \Sigma, \delta, q_0, F)$.

where

- $Q = \{q_0, q_1, q_2\}$ - set of states
- $\Sigma = \{0, 1\}$ - set of input symbols.
- $\delta: Q \times \Sigma^* \rightarrow 2^Q$ - mapping function.
- $q_0 = \{q_0\}$ - starting state.
- $F = \{q_2\}$ - Final state

- Transition diagram for all strings that begins with 0 and ends with 00.



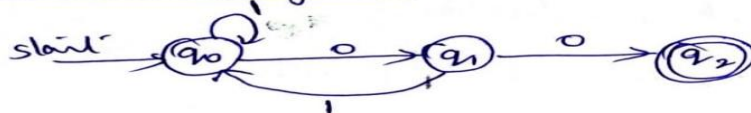
NFA, $M = (\{q_0, q_1, q_2\}, \{0, 1\}, \delta, q_0, \{q_2\})$.

- Transition Table

| states | input symbols | |
|---------|----------------|-------------|
| | 0 | 1 |
| → q_0 | $\{q_0, q_1\}$ | $\{q_0\}$ |
| q_1 | $\{q_2\}$ | \emptyset |
| * q_2 | \emptyset | \emptyset |

DFA:

Transition diagram:



Transition Table:

| state | input | |
|---------|-------------|-------------|
| | 0 | 1 |
| → q_0 | q_1 | q_0 |
| q_1 | q_2 | q_1 |
| * q_2 | \emptyset | \emptyset |

check for the validity of string : 0111100 and 01100.

input string : 0111100.

$$\delta(q_0, 0) = \{q_0, q_1\}.$$

$$\begin{aligned}\delta(q_0, 01) &= \delta(\delta(\{q_0, q_1\}, 1)) = \delta(q_0, 1) \cup \delta(q_1, 1) \\ &= \{q_0\} \cup \emptyset = \{q_0\}.\end{aligned}$$

$$\delta(q_0, 011) = \delta(q_0, 1) = \{q_0\}$$

$$\delta(q_0, 0111) = \delta(q_0, 1) = \{q_0\}.$$

$$\delta(q_0, 01111) = \delta(q_0, 1) = \{q_0\}.$$

$$\delta(q_0, 011110) = \delta(q_0, 0) = \{q_0, q_1\}.$$

$$\begin{aligned}\delta(q_0, 0111100) &= \delta(\delta(\{q_0, q_1\}, 0)) \\ &= \delta(q_0, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \{q_2\} \\ &= \{q_0, q_1, q_2\}.\end{aligned}$$

It is Accepted (q_2 is a final state).

input string : 01100.

$$\delta(q_0, 0) = \{q_0, q_1\}.$$

$$\begin{aligned}\delta(q_0, 01) &= \delta(\delta(\{q_0, q_1\}, 1)) = \delta(q_0, 1) \cup \delta(q_1, 1) \\ &= \{q_0\} \cup \emptyset = \{q_0\}.\end{aligned}$$

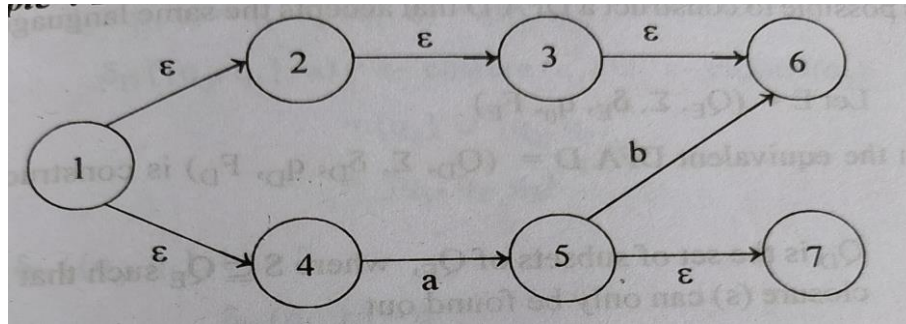
$$\delta(q_0, 011) = \delta(q_0, 0) = \{q_0, q_1\}.$$

$$\begin{aligned}\delta(q_0, 0110) &= \delta(\delta(\{q_0, q_1\}, 0)) = \delta(q_0, 0) \cup \delta(q_1, 0) \\ &= \{q_0, q_1\} \cup \{q_2\} = \{q_0, q_1, q_2\} \\ &= \{q_0, q_1, q_2\}.\end{aligned}$$

Accepted.

Or

12. Consider the following NFA - ϵ for an identifier. Consider the ϵ -closure of each state and find its equivalent DFA.



Sol: (i) $\hat{\delta}(1, \epsilon) = \{1, 2, 3, 4, 6\}$.

(ii) $\hat{\delta}(4, \epsilon) = \{4\}$.

(iii) $\hat{\delta}(5, \epsilon) = \{5, 7\}$.

(iv) $\hat{\delta}(4, a) = \epsilon\text{-closure}(\delta(\hat{\delta}(4, \epsilon), a))$
 $= \epsilon\text{-closure}(\delta(\{4\}, a) = \epsilon\text{-closure}(\{5\})$
 $= \{5, 7\}$.

(v) $\hat{\delta}(4, ab) = \epsilon\text{-closure}(\delta(\hat{\delta}(4, a), b))$
 $= \epsilon\text{-closure}(\delta(\{5, 7\}, b)$
 $= \epsilon\text{-closure}(\delta(5, b) \cup \delta(7, b))$
 $= \epsilon\text{-closure}(\{6\} \cup \emptyset)$
 $= \epsilon\text{-closure}(\{6\})$
 $= \{6\}$.

UNIT – II

13. Construct the following grammar in CNF.

$$S \rightarrow abSba / bAaB / bb$$

$A \rightarrow aa / aSAb$

$B \rightarrow Aa / abb$

Sol: Chomsky Normal Form (CNF).

1. No null and unit productions.
2. Let $G_1 = (N', \{a, b\}, S, P_1^*)$ where.

P_1 and N' are

(i) $A \rightarrow aa, B \rightarrow abb, S \rightarrow bb$ are added to P_1 .

(ii) $S \rightarrow abSba, S \rightarrow bAaB$

$A \rightarrow aSAb, B \rightarrow Aa$, yield.

$S \rightarrow C_a C_b S C_b C_a, S \rightarrow C_b A C_a B,$

$A \rightarrow C_a S A C_b, B \rightarrow A C_a, C_a \rightarrow a, C_b \rightarrow b.$

$N' = \{S, A, B, C_a, C_b\}.$

(iii) P_1 consists of $S \rightarrow C_a C_b S C_b C_a, S \rightarrow C_b A C_a B,$

$A \rightarrow C_a S A C_b, B \rightarrow A C_a, C_a \rightarrow a, C_b \rightarrow b.$
 $A \rightarrow aa, B \rightarrow abb.$

$S \rightarrow C_1 C_2 S C_2 C_1, S \rightarrow C_2 C_3 B, A \rightarrow C_1 S A C_2.$

$B \rightarrow C_3, C_1 \rightarrow C_a, C_2 \rightarrow C_b, C_3 \rightarrow A C_a.$

The resulting productions in P_1 added to P_2 .

$G_2 = (\{S, A, B, C_a, C_b, C_1, C_2, C_3\}, \{a, b\}, P_2, S).$

where P_2 consists of $S \rightarrow C_1 C_2 S C_2 C_1, S \rightarrow C_2 C_3 B, A \rightarrow C_1 S A C_2,$

$B \rightarrow C_3, C_1 \rightarrow C_a, C_2 \rightarrow C_b, C_3 \rightarrow A C_a, A \rightarrow aa, B \rightarrow abb.$

G_2 is in CNF.

Or

14. Convert the following grammar G into Greibach Normal Form (GNF).

$$S \rightarrow AB$$

$$A \rightarrow BS / b$$

$$B \rightarrow SA / a$$

Sol : Greibach Normal Form (GNF).

Sol

$$S \rightarrow AB$$

$$A \rightarrow BS \mid b.$$

$$B \rightarrow SA \mid a.$$

$$A_1 \rightarrow A_2 A_3$$

$$A_2 \rightarrow A_3 A_1 \mid b.$$

$$A_3 \rightarrow A_1 A_2 \mid a.$$

$$A_3 \rightarrow A_1 A_2 \mid a.$$

$$A_3 \rightarrow A_2 A_3 A_2 \mid a.$$

$$A_3 \rightarrow A_3 \overset{\alpha}{A_1 A_3 A_2} \mid \overset{\beta}{b A_3 A_2} \mid a$$

$$\begin{array}{l} A \rightarrow A\alpha \mid \beta \\ A \rightarrow \beta A' \mid \beta \\ B' \rightarrow \alpha A' \mid \alpha. \end{array}$$

$$A_3 \rightarrow \textcircled{b} A_3 A_2 A' \mid \textcircled{b} A' \mid \textcircled{b} A_3 A_2 \mid \textcircled{a}.$$

$$A_1 \rightarrow A_1 A_3 A_2 A' \mid A_1 A_3 A_2$$

$$A_2 \rightarrow A_3 A_1 \mid b.$$

$$A_2 \rightarrow \textcircled{b} A_3 A_2 A' A_1 \mid \textcircled{a} A' A_1 \mid \textcircled{b} A_3 A_2 A_1 \mid \textcircled{a} A_1 \mid b.$$

$$A_1 \rightarrow A_2 A_3.$$

$$A_1 \rightarrow \textcircled{b} A_3 A_2 A' A_1 A_3 \mid \textcircled{a} A' A_1 A_3 \mid \textcircled{b} A_3 A_2 A_1 A_3 \mid \textcircled{a} A_1 A_3 \mid b A_3$$

$$\begin{aligned}
 A_1 &\rightarrow b A_3 A_2 A' A, A_3 A_3 A_2 A' \mid a A' A, A_3 A_3 A_2 A' \mid \\
 &b A_3 A_2 A, A_3 A_3 A_2 A' \mid a A, A_3 A_3 A_2 A' \mid \\
 &b A_3 A_3 A_2 A' \mid b A_3 A_2 A' A, A_2 A_3 A_2 \mid \\
 &a A' A, A_3 A_3 A_2 \mid b A_3 A_2 A, A_3 A_3 A_2 \mid \\
 &a A, A_3 A_3 A_2 \mid b A_3 A_3 A_2 .
 \end{aligned}$$

It is an GNF //

UNIT – III

15. Design a Turing machine to accept the language $L = \{0^n 1^n \mid n \geq 1\}$. Draw the transition diagram.

(Also specify the instantaneous description to trace the string 0011).

Solution :

Given a finite sequence of 0's and 1's on its tape. The turing machine is designed using the following way.

- (i) M replaces the leftmost 0 by x, moves right to the leftmost 1, replacing it by y.
- (ii) Then M moves left to find the rightmost x, and moves one cell right to the leftmost 0 and repeats the cycle.
- (iii) While searching for a 1, if a blank is encountered, then M halts without accepting.
- (iv) After changing a 1 to a y, if M finds no more 0's, then M checks that no more 1's remain, accepting the string else not.

Assume the set of states $Q = \{q_0, q_1, q_2, q_3, q_4\}$

$\Sigma = \{0, 1\}$

$\Gamma = \{0, 1, x, y, B\}$

$F = \{q_4\}$

let q_0 be the initial state and at state q_0 , it replaces the leftmost 0 by x, and changes it to q_1 . At q_1 , M searches right for 1's, skipping over 0's and y's.

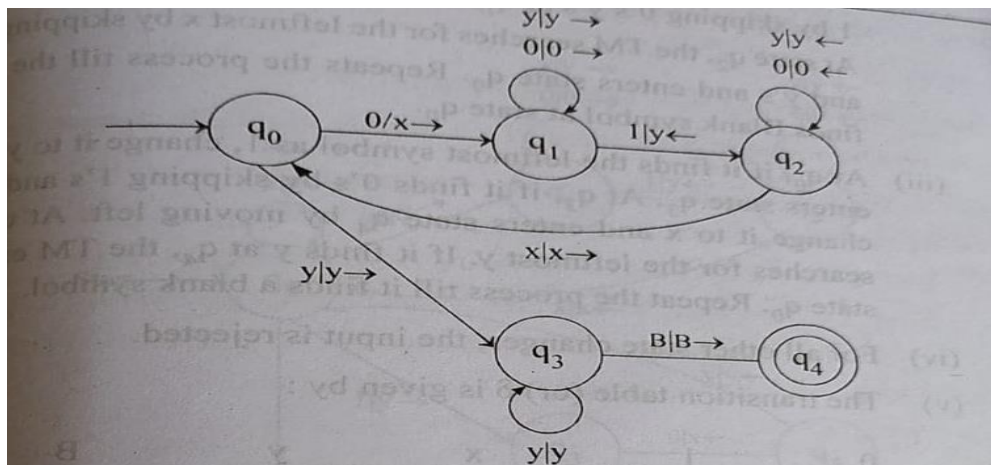


Fig. 4.15 Transition diagram for $0^n 1^n$.

$\therefore M = (Q, \Sigma, \Gamma, \delta, q_0, B, \{q_4\})$

where

$Q = \{q_0, q_1, q_2, q_3, q_4\}$

$\Sigma = \{0, 1\}$

$\Gamma = \{0, 1, x, y, B\}$

q_0 = Initial state

q_4 = Final state

δ is given in the table.

If M finds a 1, it changes it to y , entering state q_2 . From q_2 , it searches left for an x and moves right to change the state to q_0 .

At q_0 , if y is encountered, it goes to state q_3 and checks that no 1's remain. If the y 's are followed by a B , state q_4 is entered and then accepted. And for all others, M rejects.

| | 0 | 1 | x | y | B |
|-------|---------------|---------------|---------------|---------------|---------------|
| q_0 | (q_1, x, R) | — | — | (q_3, y, R) | — |
| q_1 | $(q_1, 0, R)$ | (q_2, y, L) | — | (q_1, y, R) | — |
| q_2 | $(q_2, 0, L)$ | — | (q_0, x, R) | (q_2, y, L) | — |
| q_3 | — | — | — | (q_3, y, R) | (q_4, B, R) |
| q_4 | — | — | — | — | — |

Eg :

(i) $q_0 0011 \vdash x q_1 011 \vdash x 0 q_1 11 \vdash x q_2 0 y 1 \vdash q_2 x 0 y 1 \vdash$

$x q_0 0 y 1 \vdash x x q_1 y 1 \vdash x x y q_1 1 \vdash x x q_2 y y \vdash x q_2 x y y \vdash$

$x x q_0 y y \vdash x x y q_3 y \vdash x x y y q_3 \vdash x x y y B q_4.$

Accepted.

Or

16. Show that the union of two recursive language is recursive and union of two Recursively enumerable language is recursive.

Recursive languages:

We refer to a language L as recursive if there exists a turing machine T for it. In this case, the turing machine accepts every string in language L and rejects all strings that don't match the alphabet of L .

In other words, if string S is part of the alphabet of language L , then the turing machine T will accept it otherwise the turing machine halts without ever reaching an accepting state.

Recursively enumerable languages.

Here if there is a turing machine T that accepts a language L , the language in which an enumeration procedure exists is referred to as a recursively enumerable language.

Note that some recursive languages are enumerable and some enumerable languages are recursive.

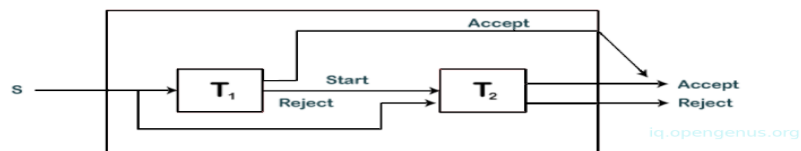
The relationship between recursive and recursively enumerable languages.



If the languages L_1 and L_2 are recursive, their union $L_1 \cup L_2$ is also recursive.

Proof:

We have two turing machines T_1 and T_2 that recognize languages L_1 and L_2 . We construct a turing machine T as shown:



T simulates T_1 and T accepts input S if T_1 accepts it also. On the other hand, if T_1 rejects, T simulates T_2 and accepts if T_2 accepts.

Both T_1 and T_2 are algorithms and therefore they will halt at some point. We conclude that T accepts $L_1 \cup L_2$.

UNIT - IV

17. Convert the grammar $S \rightarrow 0S1 / A, A \rightarrow 1A0 / S / \epsilon$ into PDA that accepts the same language by empty Stack. Check whether 1001 belongs to $N(M)$.

Sol The CFG can be first simplified by eliminating unit productions:

$$S \rightarrow 0S1 \mid 1S0 \mid \epsilon$$

Now we will convert this CFG to GNF:

$$S \rightarrow 0SX \mid 1SY \mid \epsilon$$

$$X \rightarrow 1$$

$$Y \rightarrow 0$$

The PDA can be:

$$\delta(q, \epsilon, S) = \{(q, 0SX) \mid (q, 1SY) \mid (q, \epsilon)\}$$

$$\delta(q, \epsilon, X) = \{(q, 1)\}$$

$$\delta(q, \epsilon, Y) = \{(q, 0)\}$$

$$\delta(q, 0, 0) = \{(q, \epsilon)\}$$

$$\delta(q, 1, 1) = \{(q, \epsilon)\}$$

check whether 1001 belongs to $N(M)$.

$$\delta(q, 1001, S) \vdash \delta(q, 1001, 0S1)$$

$$\vdash \delta(q, 001, 10S1)$$

$$\vdash \delta(q, 01, 010S1)$$

$$\vdash \delta(q, 1, 10S1) \quad S \rightarrow 0S1$$

$$\vdash \delta(q, \epsilon, S) \quad S \rightarrow \epsilon$$

$$\vdash \delta(q, \epsilon, \epsilon)$$

Accepted.

Or

18. Construct a PDA for the language.

A push down automata is similar to deterministic finite automata except that it has a few more properties than a DFA. The data structure used for implementing a PDA is stack. A PDA has an output associated with every input. All the inputs are either pushed into a stack or just ignored. User can perform the basic push and pop operations on the stack which is use for PDA. One of the problems associated with DFAs was that could not make a count of number of characters which were given input to the machine. This problem is avoided by PDA as it uses a stack which provides us this facility also.

A Pushdown Automata (PDA) can be defined as –

$M = (Q, \Sigma, \Gamma, \delta, q_0, Z, F)$ where

Q is a finite set of states

Σ is a finite set which is called the input alphabet

Γ is a finite set which is called the stack alphabet

δ is a finite subset of $Q \times (\Sigma \cup \{\epsilon\}) \times \Gamma \times Q \times \Gamma^*$ the transition relation.

$q_0 \in Q$ is the start state

$Z \in \Gamma$ is the initial stack symbol

$F \subseteq Q$ is the set of accepting states

Construct a PDA for language $L = \{0^n 1^m 2^m 3^n \mid n \geq 1, m \geq 1\}$

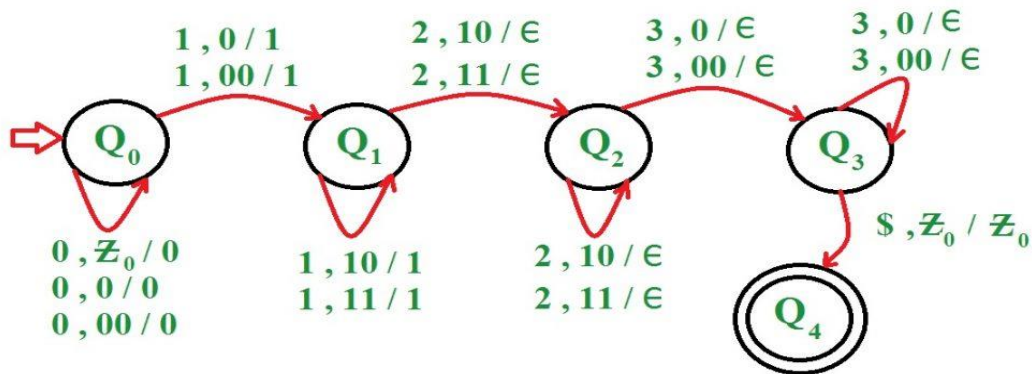
Approach used in this PDA –
First 0's are pushed into stack. Then 1's are pushed into stack. Then for every 2 as input a 1 is popped out of stack. If some 2's are still left and top of stack is a 0 then string is not accepted by the PDA. Thereafter if 2's are finished and top of stack is a 0 then for every 3 as input equal number of 0's are popped out of stack. If string is finished and stack is empty then string is accepted by the PDA otherwise not accepted.

Step-1: On receiving 0 push it onto stack. On receiving 1, push it onto stack and goto next state

Step-2: On receiving 1 push it onto stack. On receiving 2, pop 1 from stack and goto next state

Step-3: On receiving 2 pop 1 from stack. If all the 1's have been popped out of stack and now receive 3 then pop a 0 from stack and goto next state

Step-4: On receiving 3 pop 0 from stack. If input is finished and stack is empty then goto last state and string is accepted



UNIT - V

19. Find whether the following grammar is LL(1) or not.

$S \rightarrow abSa / aa / aaAb$

$A \rightarrow baAb / b$

$S \rightarrow abSa / aaAb$

$A \rightarrow baAb / b$

$FIRST(S) = \{a, a\}$

$FIRST(A) = \{b, b\}$

$FIRST\{a\} = \{a\}$

$FIRST\{b\} = \{b\}$

$FOLLOW(S) = \{ \$, a \}$

$FOLLOW(A) = \{ b \}$

| | a | b | \$ |
|---|----------------------|----------------------|--------------------------|
| S | $S \rightarrow abSa$ | | $S \rightarrow \epsilon$ |
| A | | $A \rightarrow baAb$ | |

Or

20. Consider the following grammar

$S \rightarrow AS$

$S \rightarrow b$

$A \rightarrow SA$

$A \rightarrow a$

Construct SLR parsing table and process the input string.

Sol Augmented Grammar:-

$S' \rightarrow S$
 $S \rightarrow AS$
 $S \rightarrow b$
 $A \rightarrow SA$
 $A \rightarrow a$

$goto(I_0, b)$
 $I_3: S \rightarrow b \cdot$
 $goto(I_3, A)$
 $I_4: A \rightarrow SA \cdot$
 $A \rightarrow \cdot SA$
 $S \rightarrow \cdot AS$
 $S \rightarrow \cdot b$
 $A \rightarrow \cdot SA$
 $A \rightarrow \cdot a$

$goto(I_2, A)$
 $S \rightarrow A \cdot S \Rightarrow I_2$
 $goto(I_2, a) = I_4$
 $goto(I_2, b) = I_3$
 $goto(I_5, S) = I_7$
 $goto(I_5, A) = I_2$
 $goto(I_5, a) = I_4$
 $goto(I_6, A) = I_5$
 $goto(I_6, S) = I_6$
 $goto(I_6, a) = I_4$
 $goto(I_6, b) = I_3$
 $goto(I_7, A) = I_5$
 $goto(I_7, S) = I_6$
 $goto(I_7, a) = I_4$
 $goto(I_7, b) = I_3$

Step 1:

Canonical collection of LR(0) items

$I_0: S' \rightarrow \cdot S$
 $S \rightarrow \cdot AS$
 $S \rightarrow \cdot b$
 $A \rightarrow \cdot SA$
 $A \rightarrow \cdot a$

$I_1: goto(I_0, S)$

$I_1: S' \rightarrow S \cdot$
 $S \rightarrow A \cdot S$
 $A \rightarrow SA \cdot$
 $A \rightarrow a \cdot$
 $S \rightarrow AS \cdot$
 $S \rightarrow b \cdot$

$goto(I_0, A)$

$I_2: S \rightarrow A \cdot S$
 $S \rightarrow A \cdot S$
 $A \rightarrow SA \cdot$
 $A \rightarrow a \cdot$
 $S \rightarrow AS \cdot$
 $S \rightarrow b \cdot$

$goto(I_0, a)$
 $I_4: A \rightarrow a \cdot$
 $goto(I_1, S)$
 $I_6: A \rightarrow S \cdot A$
 $A \rightarrow SA \cdot$
 $A \rightarrow a \cdot$
 $S \rightarrow AS \cdot$
 $S \rightarrow b \cdot$

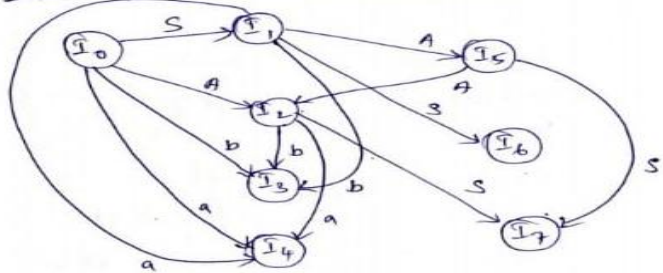
$goto(I_1, S)$
 $I_7: A \rightarrow SA \cdot$
 $S \rightarrow AS \cdot$
 $S \rightarrow A \cdot S$
 $S \rightarrow a \cdot S$
 $S \rightarrow b \cdot$
 $A \rightarrow SA \cdot$

$goto(I_1, a)$
 $A \rightarrow a \cdot = I_4$

$goto(I_1, b)$
 $S \rightarrow b \cdot \Rightarrow I_3$

$goto(I_2, S)$
 $S \rightarrow AS \cdot$
 $S \rightarrow A \cdot S$
 $A \rightarrow SA \cdot$
 $A \rightarrow a \cdot$
 $S \rightarrow AS \cdot$
 $S \rightarrow b \cdot$

Step 2: Design Finite Automata.



$FIRST(S) = \{b, a\}$

$FIRST(A) = \{a, b\}$

$FOLLOW(S) = \{\$, a, b\}$

$FOLLOW(A) = \{a, b\}$

| | Action | | | Goto | |
|---|--------|-------|----------|------|---|
| | a | b | | S | A |
| 0 | S4 | S3 | | 1 | 2 |
| 1 | S4 | S3 | Accepted | 6 | 5 |
| 2 | S4 | S3 | | 7 | 2 |
| 3 | r2 | r2 | r2 | | |
| 4 | r4 | r4 | | | |
| 5 | S4/r3 | S3/r3 | | 7 | 2 |
| 6 | S4 | S5 | | 6 | 5 |
| 7 | S4/r1 | S3/r1 | r1 | 6 | 5 |

Stack implementation of SLR parser

| <u>Stack</u> | <u>Input Buffer</u> | <u>Action</u> |
|---------------------|---------------------|---------------------------|
| \$0 | abab\$ | shift 4 |
| \$0a4 | bab\$ | reduce $A \rightarrow a$ |
| \$0A2 | bab\$ | shift 3 |
| \$0A2b3 | ab\$ | reduce $S \rightarrow b$ |
| \$0A2S7 | ab\$ | reduce $S \rightarrow AS$ |
| \$0S1 | ab\$ | shift 4 |
| \$0S1a4 | b\$ | reduce $A \rightarrow a$ |
| \$0S1A5 | b\$ | reduce $A \rightarrow SA$ |
| \$0A2 | b\$ | shift 3 |
| \$0A2b3 | \$ | reduce $S \rightarrow b$ |
| \$0A2S7 | \$ | reduce $S \rightarrow AS$ |
| \$ S 0S1 | \$ | reducer Accepted // |